



# Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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## FURTHER MATHEMATICS

9231/32

Paper 3 Further Mechanics

May/June 2021

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10 \text{ ms}^{-2}$ .

## INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.











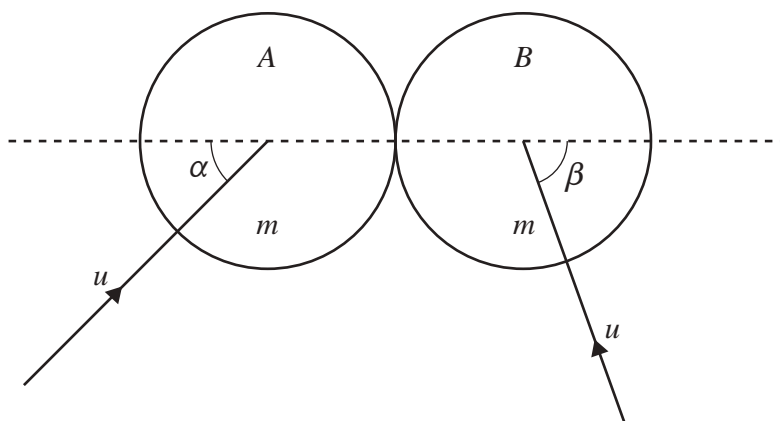






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Two uniform smooth spheres  $A$  and  $B$  of equal radii each have mass  $m$ . The two spheres are each moving with speed  $u$  on a horizontal surface when they collide. Immediately before the collision,  $A$ 's direction of motion makes an angle  $\alpha$  with the line of centres, and  $B$ 's direction of motion makes an angle  $\beta$  with the line of centres (see diagram). The coefficient of restitution between the spheres is  $\frac{1}{3}$  and  $2 \cos \beta = \cos \alpha$ .

(a) Show that the direction of motion of  $A$  after the collision is perpendicular to the line of centres.

[4]

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The total kinetic energy of the spheres after the collision is  $\frac{3}{4}mu^2$ .

**(b)** Find the value of  $\alpha$ . [4]

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(b) Find the magnitude and direction of the velocity of  $P$  one second before it strikes the plane. [4]

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